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# Full-dimensional quantum dynamics of rovibrationally inelastic scattering between CN and $\mathrm{H}_{2}$ 

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#### Abstract

We report six-dimensional (6D) potential energy surface (PES) and rovibrational scattering calculations for the $\mathrm{CN}-\mathrm{H}_{2}$ collision system. The PES was computed using the high-level ab initio spin-restricted coupled-cluster with single, double, and perturbative triple excitations-F12B method and fitted to an analytic function using an invariant polynomial method in 6D. Quantum close-coupling calculations are reported for rotational transitions in CN by $\mathrm{H}_{2}$ and $\mathrm{D}_{2}$ collisions in 6 D as well as four-dimensional (4D) within a rigid rotor model for collision energies of $1.0-1500 \mathrm{~cm}^{-1}$. Comparisons with experimental data and previous 4 D calculations are presented for CN rotational levels $j_{1}$ $=4$ and 11. For the first time, rovibrational quenching cross sections and rate coefficients of CN ( $v_{1}=1, j_{1}=0$ ) in collisions with para- and ortho $-\mathrm{H}_{2}$ are also reported in full-dimension. Agreement for pure rotational transitions is found to be good, but no experimental data on rovibrational collisional quenching for $\mathrm{CN}-\mathrm{H}_{2}$ are available. Applications of the current rotational and rovibrational rate coefficients in astrophysical modeling are briefly discussed. Published by AIP Publishing. [http://dx.doi.org/10.1063/1.4971322]


## I. INTRODUCTION

The hydrogen molecule is the dominant species in the vast majority of interstellar environments, while the cyano radical (CN) is also relatively abundant. Both may play important roles in the physics and chemistry of diffuse clouds, for example. CN is mainly observed via visible absorption in diffuse and translucent clouds, ${ }^{1,2}$ and it is also detected in the millimeter where it can be important in the chemistry of dense molecular clouds. Ever since it was identified by McKellar in 1940, ${ }^{3}$ CN has been detected in a variety of molecular clouds. ${ }^{4-8}$ For example, Wootten et al. ${ }^{4}$ reported the first observations of the $N=2-1$ line at 226.9 GHz in the circumstellar envelope of the carbon-rich star IRC +10216 and in the Orion Molecular Cloud (OMC-1). CN is also believed to be an excellent tracer of photodissociation regions (PDRs) which are environments exposed to intense ultraviolet (UV) radiation. ${ }^{9,10}$ To model the infrared radiation from CN in such environments requires a rich variety of molecular data, including inelastic rotational and vibrational collision rate coefficients, primarily due to $\mathrm{H}_{2}$. However, because of the difficulty of measurements of these quantities, numerical models often rely on theoretical rates. While state-to-state inelastic rotational (de)excitation rate coefficients due to $\mathrm{H}_{2}$ collisions were measured for the vibrationally excited state $v_{1}=2$ by Brunet et al., ${ }^{11}$ no data are available for vibrationally inelastic transitions in CN induced by $\mathrm{H}_{2}$.

Due to its fundamental and astrophysical importance, the $\mathrm{CN}-\mathrm{H}_{2}$ collisional system has been the subject of many
theoretical ${ }^{12-18}$ and experimental ${ }^{11,19}$ studies. An early fourdimensional (4D) potential energy surface (PES) within the rigid-rotor model was obtained by Kaledin et al. ${ }^{12}$ and applied to a study of the spectroscopy of the $\mathrm{CN}-\mathrm{H}_{2}$ van der Waals complex. More recently, Kalugina et al. ${ }^{14,15}$ calculated a 4D PES using the partially spin-restricted coupled-cluster with single, double, and perturbative triple excitations $(\operatorname{RCCSD}(\mathrm{T}))$ method and an aug-cc-pVTZ basis set augmented by $3 s, 2 p$, $1 d$ bond functions. Fine- and hyperfine-resolved collisional excitation calculations of $\mathrm{CN}\left(v_{1}=0\right)$ with para $-\mathrm{H}_{2}\left(v_{2}=0\right.$, $j_{2}=0$ ) were performed, but using a two-dimensional (2D) PES obtained by averaging the 4D PES over the $\mathrm{H}_{2}$ angular degrees of freedom. Later, the 4D PES of Kalugina et al. ${ }^{14,15}$ was used in close-coupling (CC) calculations of rotational de-excitation cross section of $\mathrm{CN}\left(v_{1}=0\right)$ by para- and ortho $-\mathrm{H}_{2} .{ }^{15}$ In both PES and scattering calculations, ${ }^{14,15}$ fixed bond distances (i.e., equilibrium bond distance of CN at $r_{1}=2.2144 \mathrm{a}_{0}$ and vibrationally averaged bond distance of $\mathrm{H}_{2}$ at $r_{2}=1.4487 \mathrm{a}_{0}$ ) were adopted. Recently, the 4D PES of Kalugina and Lique was also applied to calculate fine- and hyperfine-resolved rotational excitation rate coefficients of CN with para- and ortho- $\mathrm{H}_{2}{ }^{17}$ and of CN isotopologues, ${ }^{13} \mathrm{CN}$ and $\mathrm{C}^{15} \mathrm{~N}$, by para $-\mathrm{H}_{2} .{ }^{18}$

To go beyond the rigid-rotor approximation, in this work we have constructed a full dimensional (6D) PES for the $\mathrm{CN}-\mathrm{H}_{2}$ system and carried out comprehensive CC calculations of state-to-state cross sections in an effort to initiate the development of a complete database of rovibrational quenching rate coefficients. In Secs. II-V, the 6D PES calculations, the adopted scattering approach, and the results are
discussed. Conclusions are presented in Sec. VI. Transitions at the fine- or hyperfine-resolved level are not considered here.

## II. THE POTENTIAL ENERGY SURFACE

The electronic ground state interaction potential of $\mathrm{CN}-\mathrm{H}_{2}$ was computed using the explicitly correlated coupledcluster (RCCSD(T)-F12B) method, ${ }^{20,21}$ with an aug-cc-pVTZ basis, ${ }^{22}$ as implemented in MOLPRO 2010.1. ${ }^{23}$ The interaction energies were calculated using the supermolecular approach in which the counter-poise (CP) ${ }^{24}$ correction was employed to reduce the basis set superposition error (BSSE). ${ }^{25}$ To construct the PES, the computations were performed on a 6D grid using Jacobi coordinates as shown in Fig. 1. The radial coordinate $R$ denotes the distance between the center-of-masses of CN and $\mathrm{H}_{2}$, while $r_{1}$ and $r_{2}$ represent the bond lengths of CN and $\mathrm{H}_{2}$, respectively. The angular coordinates $\theta_{1}$ and $\theta_{2}$ denote, respectively, the angle between $\vec{r}_{1}$ and $\vec{R}$ and $\vec{r}_{2}$ and $\vec{R}$, while $\phi$ denotes the out-of-plane dihedral angle. For the potential energy calculations, the bond lengths of $\mathrm{H}_{2}$ and CN spanned the range $1.1011-1.8011 \mathrm{a}_{0}$ and 2.0184-2.5184 $\mathrm{a}_{0}$, respectively. $R$ is scanned from 5 to $21 \mathrm{a}_{0}$ with a stepsize of $0.5 \mathrm{a}_{0}$ for $R<8 \mathrm{a}_{0}$ and $1.0 \mathrm{a}_{0}$ for $R>8 \mathrm{a}_{0}$. The angle $\theta_{1}$ ranges from $0^{\circ}$ to $180^{\circ}$ with a step-size of $22.5^{\circ}$, and $\theta_{2}$ and $\phi$ have range $0^{\circ}$ to $180^{\circ}$ and $0^{\circ}$ to $90^{\circ}$, respectively, with a step-size of $30^{\circ}$. The range of $r_{1}$ and $r_{2}$ allows for the treatment of vibrational excitation up to $v_{1}=2$ for CN , but only for $v_{2}=0$ for $\mathrm{H}_{2}$, and as the bond lengths do not approach dissociation, rearrangement channels (e.g., to form HCN) are excluded from consideration on this PES. While the barrier to reaction is around $1260 \mathrm{~cm}^{-1}(3.6 \mathrm{kcal} / \mathrm{mol})$, which is comparable to the $\mathrm{CN}\left(v_{1}=1\right)$ excitation energy, CN plays the role of a spectator in the reaction dynamics because the effective barrier at the saddle point increases by the same energy as the $\mathrm{CN}\left(v_{1}=1\right)$ excitation energy. As a consequence, reaction channels are not incorporated into the PES or scattering.

An invariant polynomial method ${ }^{26,27}$ has been used to fit the $6 \mathrm{D} \mathrm{CN}-\mathrm{H}_{2}$ interaction PES, which is expanded in the form
$V\left(y_{1} \cdots y_{6}\right)=\sum_{n_{1} \cdots n_{6}}^{N} c_{n_{1} \cdots n_{6}} y_{1}^{n_{1}} y_{6}^{n_{6}}\left[y_{2}^{n_{2}} y_{3}^{n_{3}} y_{4}^{n_{4}} y_{5}^{n_{5}}+y_{2}^{n_{5}} y_{3}^{n_{4}} y_{4}^{n_{3}} y_{5}^{n_{2}}\right]$,
where $y_{i}=e^{-0.5 d_{i}}$ is a Morse-type variable, $d_{i}$ are the internuclear distances (in atomic units) between two atoms, $d_{1}=d_{\mathrm{HH}^{\prime}}$, $d_{2}=d_{\mathrm{NH}^{\prime}}, d_{3}=d_{\mathrm{CH}^{\prime}}, d_{4}=d_{\mathrm{CH}}, d_{5}=d_{\mathrm{NH}}$, and $d_{6}=d_{\mathrm{CN}}$. The total power of the polynomial, $N=\sum_{i=1}^{7} n_{i}$, was restricted to 7 .


FIG. 1. The six-dimensional Jacobi coordinates for $\mathrm{CN}-\mathrm{H}_{2}$.

TABLE I. Global and local minima on the 4D PESs. $V$ in $\mathrm{cm}^{-1}, R$ in bohr.

|  | V6ES-4D | Reference 15 | Reference 12 |
| :--- | :--- | :--- | ---: |
| Global | $\mathrm{V}=-122.51$ | $\mathrm{~V}=-121.36$ | -100.84 |
|  | $\mathrm{R}=7.21$ | $\mathrm{R}=7.23$ | 7.44 |
| Local | $\mathrm{V}=-81.98$ | $\mathrm{~V}=-83.86$ | -68.44 |
|  | $\mathrm{R}=7.41$ | $\mathrm{R}=7.39$ | 7.52 |

The fit for the expansion coefficients $c_{n_{1} \ldots n_{6}}$ was performed using a weighted least-squares method for interaction energies up to $3000 \mathrm{~cm}^{-1}$. The root-mean-square (RMS) error in the PES fit was $3.67 \mathrm{~cm}^{-1}$, which included 84734 ab initio points. The 6D interaction PES, $V\left(R, r_{1}, r_{2}, \theta_{1}, \theta_{2}, \phi\right)$, hereafter referred to as V6ES, can be averaged over the ground-state or excited vibrational wave functions of CN and $\mathrm{H}_{2}$ to obtain 4D vibrationally averaged PESs, $V\left(R, \theta_{1}, \theta_{2}, \phi\right)$. However, V6ES was used in the majority of the scattering calculations. The comparison of the global and local minima on the vibrationally averaged V6ES-4D PES and the 4D PESs of Kalugina et al. ${ }^{15}$ and Kaledin et al. ${ }^{12}$ is given in Table I. Note that this is not an exact comparison as the 4D PESs were constructed differently.

Some features of the fitted V6ES PES are illustrated in Figs. 2-4. Fig. 2 displays the $R$ dependence of V6ES for various angles and bond distances fixed at $r_{1}=r_{\mathrm{e}}(\mathrm{CN})=2.2144 \mathrm{a}_{0}$ and $r_{2}=r_{\mathrm{e}}\left(\mathrm{H}_{2}\right)=1.4011 \mathrm{a}_{0}$. The computed ab initio potential energy points are also displayed as symbols. Fig. 3 shows twodimensional contour plots in $\theta_{1}$ and $\theta_{2}$ for the V6ES PES. The CN and $\mathrm{H}_{2}$ bond lengths are fixed at their equilibrium distances for $R=3.0,3.5,4.0$, and $6.0 \AA, \phi=0^{\circ}, 45^{\circ}$, and $90^{\circ}$. This figure can be compared to Fig. 3 of Kalugina et al. ${ }^{15}$ and Fig. 2 of Kaledin et al. ${ }^{14}$ The current Fig. 4 depicts the anisotropy of the V6ES potential in $\theta_{1}$ for various $\phi$. Here $\theta_{1}$ describes the orientation of CN ; the anisotropy with respect to $\theta_{1}$ is large.


FIG. 2. $R$ dependence of the interaction potential V6ES for representative slices with bond lengths fixed as indicated in the text and $\left(\theta_{1}, \theta_{2}, \phi\right)$ $=\left(0^{\circ}, 0^{\circ}, 0^{\circ}\right),\left(180^{\circ}, 0^{\circ}, 0^{\circ}\right),\left(180^{\circ}, 90^{\circ}, 0^{\circ}\right)$, and $\left(90^{\circ}, 90^{\circ}, 90^{\circ}\right)$. V6ES fit (lines), computed ab initio energy points (symbols).


FIG. 3. Contour plots of $\theta_{1}$ and $\theta_{2}$. CN and $\mathrm{H}_{2}$ bond distances $r_{1}=2.2144$ and $r_{2}=1.4011 \mathrm{a}_{0}$. The rows correspond to $R=3.0,3.5,4.0$, and $6.0 \AA$, while the columns correspond to $\phi=0^{\circ}, 45^{\circ}$, and $90^{\circ}$.

## III. SCATTERING METHODS

In the quantum-mechanical description of inelastic molecular scattering, the theory for the collision of two ${ }^{1} \Sigma$ diatomic molecules within the rigid rotor and vibrating rotor models was developed ${ }^{28-31}$ based on the close-coupling
(CC) formulation of Arthurs and Dalgarno. ${ }^{32}$ Recently the theory has been implemented for the full-dimensional study of the vibrationally inelastic scattering between two diatomic molecules. ${ }^{33-35}$ Here, we apply this formalism for the $\mathrm{CN}+\mathrm{H}_{2}$ system by approximating CN as a ${ }^{1} \Sigma$ molecule,


FIG. 4. Comparison of the $\theta_{1}$ dependence of the V6ES surface for $\phi=0^{\circ}$, $45^{\circ}, 90^{\circ}, 135^{\circ}$, and $180^{\circ} . R=6.0 \mathrm{a}_{0}, \theta_{2}=45^{\circ}, r_{1}=2.2144 \mathrm{a}_{0}$, and $r_{2}$ $=1.4011 \mathrm{a}_{0}$.
hence the rotational quantum number $N_{1}=j_{1}$ since we neglect spin. In the scattering calculations, the interaction PES $V\left(R, r_{1}, r_{2}, \theta_{1}, \theta_{2}, \phi\right)$ was expanded in the form

$$
\begin{align*}
V\left(R, r_{1}, r_{2}, \theta_{1}, \theta_{2}, \phi\right)= & \sum_{\lambda_{1} \lambda_{2} \lambda_{12}} A_{\lambda_{1}, \lambda_{2}, \lambda_{12}}\left(r_{1}, r_{2}, R\right) \\
& \times Y_{\lambda_{1}, \lambda_{2}, \lambda_{12}}\left(\hat{r}_{1}, \hat{r}_{2}, \hat{R}\right) \tag{2}
\end{align*}
$$

where $Y_{\lambda_{1}, \lambda_{2}, \lambda_{12}}$ is a bi-spherical harmonic function given by

$$
\begin{align*}
Y_{\lambda_{1}, \lambda_{2}, \lambda_{12}}\left(\hat{r}_{1}, \hat{r}_{2}, \hat{R}\right)= & \sum_{m_{\lambda_{1}} m_{\lambda_{2}} m_{\lambda_{12}}}\left\langle\lambda_{1} m_{\lambda_{1}} \lambda_{2} m_{\lambda_{2}} \mid \lambda_{12} m_{\lambda_{12}}\right\rangle \\
& \times Y_{\lambda_{1} m_{\lambda_{1}}}\left(\hat{r}_{1}\right) Y_{\lambda_{2} m_{\lambda_{2}}}\left(\hat{r}_{2}\right) Y_{\lambda_{12} m_{\lambda_{12}}}^{*}(\hat{R}), \tag{3}
\end{align*}
$$

where $0 \leq \lambda_{1} \leq 8,0 \leq \lambda_{2} \leq 4$, and only even values of $\lambda_{2}$ are retained due to the symmetry of $\mathrm{H}_{2}$.

We use the term combined molecular state (CMS) to describe a combination of rovibrational states of the $\mathrm{CN}-\mathrm{H}_{2}$ scattering system. A CMS, denoted as ( $v_{1} j_{1} v_{2} j_{2}$ ), represents a unique quantum state before or after a collision: $v=v_{1} v_{2}$ and $j=j_{1} j_{2}$ denote the vibrational and rotational quantum numbers of the two molecules.

The rovibrational state-to-state cross section as a function of collision energy $E$ is given by

$$
\begin{align*}
\sigma_{v_{1} j_{1} v_{2} j_{2} \rightarrow v_{1}^{\prime} j_{1}^{\prime} 1_{2}^{\prime} j_{2}^{\prime}}(E)= & \frac{\pi}{\left(2 j_{1}+1\right)\left(2 j_{2}+1\right) k^{2}} \\
& \times \sum_{j_{12} j_{12}^{\prime} l l^{\prime} J \varepsilon_{I}}(2 J+1) \mid \delta_{v_{1} j_{1} v_{2} j_{2} l, v_{1}^{\prime} j_{1}^{\prime} v_{1}^{\prime} j_{2}^{\prime} l^{\prime}} \\
& -\left.S_{v_{1} j_{1} v_{2} j_{2} l, v_{1}^{\prime} j_{1}^{\prime} v_{1}^{\prime} j_{2}^{\prime} l^{\prime}}^{J l_{I}}(E)\right|^{2} \tag{4}
\end{align*}
$$

where $\left(v_{1} j_{1} v_{2} j_{2}\right)$ and $\left(v_{1}^{\prime} j_{1}^{\prime} v_{2}^{\prime} j_{2}^{\prime}\right)$ denote the initial and final CMSs, respectively, and $l$ is the orbital angular momentum quantum number. The total angular momentum of the collision system is given by $\vec{J}=\vec{l}+\vec{j}_{12}$ with $\vec{j}_{12}=\vec{j}_{1}+\vec{j}_{2}$ and $k=\sqrt{2 \mu E / \hbar^{2}}$ is the wave vector with respect to the initial channel.

For a given $\mathrm{H}_{2}$ transition, $j_{2} \rightarrow j_{2}^{\prime}$, the total vibrational quenching cross section of CN from $v_{1} \rightarrow v_{1}^{\prime}$ can be obtained by summing over the final rotational levels $j_{1}^{\prime}$ of CN in vibrational state $v_{1}^{\prime}$,

$$
\begin{equation*}
\sigma_{v_{1} j_{1} v_{2} j_{2} \rightarrow v_{1}^{\prime} v_{2}^{\prime} j_{2}^{\prime}}^{\mathrm{T}}(E)=\sum_{j_{1}^{\prime}} \sigma_{v_{1} j_{1} v_{2} j_{2} \rightarrow v_{1}^{\prime} j_{1}^{\prime} v_{2}^{\prime} j_{2}^{\prime}}(E) . \tag{5}
\end{equation*}
$$

In this work, $\mathrm{H}_{2}$ is taken to remain in its ground vibrational state, $v_{2}=v_{2}^{\prime}=0$. However, the CN total vibrational quenching cross sections were calculated for both elastic $\left(j_{2}^{\prime}=j_{2}\right)$ and inelastic $\left(j_{2}^{\prime} \neq j_{2}\right) \mathrm{H}_{2}$ transitions.

All CC scattering calculations were carried out using the TwoBC code ${ }^{36}$ with the coupled-channel equations propagated using the log-derivative method of Johnson ${ }^{37}$ and Manolopou$\operatorname{los}^{38}$ with a radial step-size of $\Delta R=0.05 \mathrm{a}_{0}$ and the range of $R$ propagation from 5 to $21 a_{0}$. The number of discrete variable representation points $N_{r 1}$ and $N_{r 2}$; the number of points in $\theta_{1}$ and $\theta_{2}$ for Gauss-Legendre quadrature, $N_{\theta_{1}}$ and $N_{\theta_{2}}$; and the number of points in $\phi$ for Chebyshev quadrature, $N_{\phi}$, used to project out the potential expansion coefficients are presented in Table II. The basis sets used in the pure rotational and rovibrational scattering calculations are also presented in Table II.

The state-to-state rate coefficients at a temperature $T$ can be obtained by thermally averaging the corresponding integral cross sections over a Maxwellian kinetic energy distribution,

$$
\begin{align*}
k_{v_{1} j_{1} v_{2} j_{2} \rightarrow v_{1}^{\prime} j_{1}^{\prime} v_{2}^{\prime} j_{2}^{\prime}}(T)= & \left(\frac{8}{\pi \mu \beta}\right)^{1 / 2} \beta^{2} \int_{0}^{\infty} E \sigma_{v_{1} j_{1} v_{2} j_{2} \rightarrow v_{1}^{\prime} j_{1}^{\prime} v_{2}^{\prime} j_{2}^{\prime}}(E) \\
& \times \exp (-\beta E) d E \tag{6}
\end{align*}
$$

TABLE II. Parameters used in the TwoBC scattering calculations.

|  | Basis set ${ }^{\mathrm{a}}$ | $N_{\theta_{1}}$ | $N_{\theta_{2}}$ | $N_{\phi}$ | $N_{r 1}$ | $N_{r 2}$ | $\lambda_{1}$ | $\lambda_{2}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6D rotational calculation |  |  |  |  |  |  |  |  |
| para $-\mathrm{H}_{2}-\mathrm{CN}$ | $j_{1}=20, j_{2}=2$ | 12 | 12 | 8 | 18 | 18 | 8 | 4 |
| ortho $-\mathrm{H}_{2}-\mathrm{CN}$ | $j_{1}=20, j_{2}=3$ | 12 | 12 | 8 | 18 | 18 | 8 | 4 |
| 6D rovibrational calculation |  |  |  |  |  |  |  |  |
| para $-\mathrm{H}_{2}-\mathrm{CN}$ | $[(0,22 ; 1,20)(0,2)]$ | 12 | 12 | 8 | 18 | 18 | 8 | 4 |
| para $-\mathrm{H}_{2}-\mathrm{CN}$ | $[(0,22 ; 1,20)(0,3)]$ | 12 | 12 | 8 | 18 | 18 | 8 | 4 |

${ }^{\text {a }}$ Basis set $\left[\left(v_{1}=0, j_{v 1}=0 ; v_{1}=1, j_{v_{1}=1}\right)\left(v_{2}=0, j_{v_{2}}=0\right)\right]$ is presented by the maximum rotational quantum number $j_{v_{1}}$ and $j_{v_{2}}$ included in each relevant vibrational level $v_{1}$ and $v_{2}$ for CN and $\mathrm{H}_{2}$, respectively.
where $\mu$ is the reduced mass of the $\mathrm{CN}-\mathrm{H}_{2}$ complex, $\beta=\left(k_{\mathrm{B}} T\right)^{-1}$, and $k_{\mathrm{B}}$ is Boltzmann's constant.

## IV. RESULTS

## A. Pure rotational scattering

We first consider the rotational transitions of CN in collisions with $\mathrm{H}_{2}$ and $\mathrm{D}_{2}$ when the molecules remain in their ground vibrational states $v_{1}=v_{2}=v_{1}^{\prime}=v_{2}^{\prime}=0$,

$$
\begin{aligned}
\mathrm{CN}\left(v_{1}=0, j_{1}\right)+\mathrm{H}_{2}\left(v_{2}=0, j_{2}\right) \rightarrow & \mathrm{CN}\left(v_{1}^{\prime}=0, j_{1}^{\prime}\right) \\
& +\mathrm{H}_{2}\left(v_{2}^{\prime}=0, j_{2}^{\prime}\right)
\end{aligned}
$$

and

$$
\begin{aligned}
\mathrm{CN}\left(v_{1}=0, j_{1}\right)+\mathrm{D}_{2}\left(v_{2}=0, j_{2}\right) \rightarrow & \mathrm{CN}\left(v_{1}^{\prime}=0, j_{1}^{\prime}\right) \\
& +\mathrm{D}_{2}\left(v_{2}^{\prime}=0, j_{2}^{\prime}\right)
\end{aligned}
$$

Full-dimensional calculations using TwoBC with V6ES and rigid rotor approximation calculations using MOLSCAT ${ }^{39}$ with vibrationally averaged 4D PESs have been performed to obtain the rotational excitation and de-excitation cross sections of CN in collisions with $\mathrm{H}_{2}$. For CN with $\mathrm{D}_{2}$, only rigid-rotor approximation calculations using vibrationally averaged 4D PESs are carried out. Three vibrationally averaged 4D PESs in the CN ground and excited vibrational states $v_{1}=0,1$, and 2 , referred to as V4H2-0, V4H2-1, and V4H2-2, are computed for $\mathrm{CN}-\mathrm{H}_{2}$. For $\mathrm{CN}-\mathrm{D}_{2}$, the vibrationally averaged 4D PESs are referred to as V4D2-0, V4D2-1, and V4D2-2. In constructing these 4D PESs, $\mathrm{H}_{2}$ and $\mathrm{D}_{2}$ are in their ground vibrational state $v_{2}=0$.

The initial rotational state of CN was taken to be $j_{1}=4$ and 11 to make comparisons with available measurements as described below. For para $-\mathrm{H}_{2}$ and ortho- $\mathrm{D}_{2}$, rotational levels $j_{2}=0$ and 2 were included in the basis set while for ortho $-\mathrm{H}_{2}$ and para- $\mathrm{D}_{2}, j_{2}=1$ and 3 were included.

Rotational excitation and de-excitation cross sections of $\mathrm{CN}\left(v_{1}=0, j_{1}=4\right)$ in collisions with para- $\mathrm{H}_{2}\left(v_{2}=0, j_{2}\right.$ $=0,2)$ and ortho $-\mathrm{H}_{2}\left(v_{2}=0, j_{2}=1\right)$ have been computed
for collision energies ranging from 1.0 to $1500 \mathrm{~cm}^{-1}$. In Figs. 5-7, the calculated de-excitation cross sections using V6ES and V4H2-0 are compared with the 4D results of Kalugina et al. ${ }^{15}$ It can be seen that the 6D V6ES and 4D V4H2-0 PESs yield nearly identical results. The cross sections for deexcitation from $j_{1}=4$ are seen to be in good agreement with the results of Kalugina et al.

Brunet et al. ${ }^{11}$ measured the rotational inelastic, but vibrationally elastic, state-to-state rate coefficients of CN $\left(X^{2} \Sigma^{+}, v_{1}=2\right)$ due to collisions with normal $\mathrm{H}_{2}$ and $\mathrm{D}_{2}$. For comparison, the state-to-state rotational excitation and deexcitation rate coefficients of $\mathrm{CN}\left(v_{1}=0, j_{1}=4\right.$ and 11) in collisions with $\mathrm{H}_{2}$ and $\mathrm{D}_{2}$ with $v_{2}=0, j_{2}=0,1,2$ are computed using Eq. (6). The Boltzmann average, over the $\mathrm{H}_{2}$ and $\mathrm{D}_{2}$ rotational levels, of the state-to-state rate coefficients $k\left(j_{1} j_{2}\right)$ was then obtained with the partition function $Q$ of the first three rotational states of $\mathrm{H}_{2}$ and $\mathrm{D}_{2}\left(j_{2}=0,1,2\right)$ and given by

$$
\begin{equation*}
\bar{k}\left(j_{1}\right)=\frac{\sum_{j_{2}=0}^{2} w_{j_{2}}\left(2 j_{2}+1\right) e^{-\epsilon_{j_{2}} / k T} k\left(j_{1} j_{2}\right)}{Q} \tag{7}
\end{equation*}
$$

where

$$
\begin{equation*}
Q=\sum_{j_{2}=0}^{2} w_{j_{2}}\left(2 j_{2}+1\right) e^{-\epsilon_{j_{2}} / k T} \tag{8}
\end{equation*}
$$

$k\left(j_{1} j_{2}\right)$ is the rate coefficients from initial CMS $\left(0 j_{1} 0 j_{2}\right)$, $\epsilon_{j_{2}}=B_{0} j_{2}\left(j_{2}+1\right)$, the rotational constant $B_{0}$ is $59.3219 \mathrm{~cm}^{-1}$ for $\mathrm{H}_{2}$ and $29.9043 \mathrm{~cm}^{-1}$ for $\mathrm{D}_{2}$, and $w_{j 2}$ is the spin degeneracy, $w_{j 2}=3$ for ortho $-\mathrm{H}_{2}$ and para $-\mathrm{D}_{2}$ and 1 for para $-\mathrm{H}_{2}$ and ortho- $\mathrm{D}_{2}$.

In Figs. 8 and 9 we compare the present rate coefficients with measurements ${ }^{11}$ and the theoretical results of Kalugina et al. ${ }^{15}$ For collisions with normal $\mathrm{H}_{2}$ and $j_{1}=4$, the results of full-dimensional calculations using V6ES and rigid-rotor approximation calculations using vibrationally averaged PESs V4H2-0, V4H2-1, and V4H2-2 are displayed in Fig. 8(a). The 4D PESs yield very similar scattering results, which are also comparable to the 6 D results. Due to the degeneracy


FIG. 5. Rotational de-excitation cross sections for $\mathrm{CN}\left(v_{1}=0, j_{1}=4\right)+\mathrm{H}_{2}\left(v_{2}\right.$ $\left.=0, j_{2}=0\right) \rightarrow \mathrm{CN}\left(v_{1}^{\prime}=0, j_{1}^{\prime}\right)+\mathrm{H}_{2}\left(v_{2}^{\prime}\right.$ $\left.=0, j_{2}^{\prime}=0\right), j_{1}^{\prime}=0,1,2$, and 3 with initial CMS (0400). Current 6D (lines) and 4D0 (triangles) results and 4D calculations of Ref. 15 (circles).


FIG. 6. Same as Figure 5 except for $j_{2}$ $=j_{2}^{\prime}=1$, i.e., initial CMS (0401).
factors and assumed relative rotational populations given by Equation (7), the rate coefficients for normal $-\mathrm{H}_{2}$ are dominated by ortho $-\mathrm{H}_{2}$ transitions. Therefore, while Fig. 5 displays an even $\Delta j_{1}$ propensity rule for para $-\mathrm{H}_{2}$, applicable for a near-homonuclear molecule like CN , an exponential energy-gap-law behavior is evident for ortho $-\mathrm{H}_{2}$ cross sections in Fig. 6. As a consequence, any evidence of an even $\Delta j$ propensity is washed-out in Fig. 8 with the result that $\Delta j_{1}= \pm 1$ dominates. For $j_{1}=11$, presented in Fig. 8(b), the even $\Delta j_{1}$ propensity is partially recovered, though $\Delta j_{1}= \pm 1$ transitions give the largest rate coefficients.

For both $j_{1}=4$ and 11 , the comparison of the present rate coefficients with experiment and the theoretical results of Kalugina et al. ${ }^{15}$ shows good agreement particularly in light of the fact that this is an absolute value comparison. The exception
occurs for $\Delta j_{1}= \pm 1$ transitions where noticeable differences are found between the experiment and all calculations. The calculations of Kalugina et al. ${ }^{15}$ are somewhat closer to the measurements which are mostly due to their slightly larger (0401) to (0301) cross section (see bottom right panel of Fig. 6).

Fig. 9 shows similar comparisons between our theoretical results of CN in collision with $\mathrm{D}_{2}$ and measurements. ${ }^{11}$ The results from three vibrationally averaged 4D PESs, V4D2-0, V4D2-1, and V4D2-2 are very similar for both $j_{1}=4$ and 11 , except that V4D2-2 gives smaller rate coefficients for $\Delta j_{1}= \pm 1$ transitions.

While the measurement was performed for vibrationally excited $\mathrm{CN}\left(v_{1}=2\right)$, calculations which used $v_{1}=0$, though for vibrationally averaged PESs, are not direct comparisons. We explored whether this was an issue by repeating our 4D


FIG. 7. Same as Figure 5 except for $j_{2}$ $=j_{2}^{\prime}=2$, i.e., initial CMS (0402).


FIG. 8. Inelastic rotational rate coefficients for CN at $T=295 \mathrm{~K}$ for a statistical population of $\mathrm{H}_{2}\left(v_{2}=0, j_{2}=0,1\right)$, i.e., normal- $\mathrm{H}_{2}$. (a) $j_{1}=4$, (b) $j_{1}=11$. Experiment ${ }^{11} v_{1}=2$ (solid circles), 4D theory ${ }^{15} v_{1}=0$ (stars), and current 6D and 4D theory $v_{1}=0$ (open triangles and open circles), $v_{1}=1$ (open squares), and $v_{1}=2$ (open diamonds).
calculations on $v_{1}=1$ and 2 vibrationally averaged PESs. Figs. 8 and 9 demonstrate that rotational transitions are nearly independent of $v_{1}$, except as noted above, the $\Delta j_{1}= \pm 1$ transitions are somewhat smaller for $\mathrm{D}_{2}$ collisions on the V4D2-2, i.e., $v_{1}=2$ surface. This might be related to the partial recovery of an even $\Delta j_{1}$ propensity for ortho- $\mathrm{D}_{2}$ collisions. Nevertheless, it appears that CN is sufficiently harmonic whose dependence on $v_{1}$ for pure rotational transitions is small.


FIG. 9. Inelastic rotational rate coefficients for CN at $T=295 \mathrm{~K}$ for a statistical population of $\mathrm{D}_{2}\left(v_{2}=0, j_{2}=0\right.$, 1), i.e., normal- $\mathrm{D}_{2}$. (a) $j_{1}=4$, (b) $j_{1}$ $=11$. Experiment ${ }^{11} v_{1}=2$ (solid circles) and current 4D theory $v_{1}=0$ (open circles), $v_{1}=1$ (open squares), and $v_{1}=2$ (open triangles).

Returning to the experiment, they were state-to-state measurements performed by laser probing the CN level populations and then using a master equation analysis to extract rate coefficients. For $v_{1}>0$, the level populations may also be quenched by reactive scattering to $\mathrm{H}+\mathrm{HCN}$ and vibrational de-excitation, which are not considered in the experimental modeling. Vibrational quenching is typically many orders of magnitude smaller than rotational quenching but may become competitive for a quasi-resonant transition as found for CO- $\mathrm{H}_{2}{ }^{35}$ (e.g., the $1002 \rightarrow 0006+83 \mathrm{~cm}^{-1}$ transition, in CMS notation). For $\mathrm{CN}-\mathrm{H}_{2}$, the quasi-resonant transitions 1002 $\rightarrow 0006-18 \mathrm{~cm}^{-1}$ and $2002 \rightarrow 1006-45 \mathrm{~cm}^{-1}$ are potentially relevant to the Brunet et al. ${ }^{11}$ measurements. Both processes are slightly endoergic and will be studied in future work.

## B. Scattering calculations for vibrational quenching

Full-dimensional quantum CC calculations of rovibrational cross sections were carried out for initial CMSs $\left(100 j_{2}\right)$, for para $-\mathrm{H}_{2}\left(j_{2}=0\right)$ and ortho $-\mathrm{H}_{2}\left(j_{2}=1\right)$ with collision energies ranging from 1 to $1000 \mathrm{~cm}^{-1}$. In Figs. 10 and 11 the state-to-state quenching cross section to final states $\left(0 j_{1}^{\prime} 0 j_{2}\right)$, $j_{1}^{\prime}=0,2,4, \ldots, 24$ are shown for para- and ortho- $\mathrm{H}_{2}$, respectively, where $j_{2}=j_{2}^{\prime}$. The cross sections have similar behavior and display resonances at low energies due to quasibound states of the collision complex. Small $\left|\Delta j_{1}\right|=\left|j_{1}^{\prime}-j_{1}\right|$ transitions dominate the quenching with the cross sections generally decreasing with increasing $j_{1}^{\prime}$ with that for $j_{1}^{\prime}=0$ being the largest. This indicates that the cross section is dominated by the strength of the interaction terms $A_{\lambda_{1}, \lambda_{2}, \lambda_{12}}$ and not by the asymptotic channel energy gaps.

The total cross sections $\sigma_{v_{1} j_{1} v_{2} j_{2} \rightarrow v_{1}^{\prime} v_{2}^{\prime} j_{2}^{\prime}}^{\mathrm{T}}(E)$ for CN vibrational quenching from $v_{1}=1 \rightarrow v_{1}^{\prime}=0$ are given in Fig. 12. Fig. 12(a) shows the total cross section from (1000) to CN $\left(v_{1}^{\prime}=0\right)+$ para $-\mathrm{H}_{2}\left(j_{2}^{\prime}=0,2\right)$, while Fig. 12(b) displays the total cross section from (1001) to $\mathrm{CN}\left(v_{1}^{\prime}=0\right)+$ ortho $-\mathrm{H}_{2}$ $\left(j_{2}^{\prime}=1,3\right)$. The total vibrational quenching cross section display orbiting resonances between collision energies of 1.0 and $100 \mathrm{~cm}^{-1}$. However, the magnitude of the resonances are suppressed for $\mathrm{H}_{2}$ elastic processes, $j_{2}=j_{2}^{\prime}$. For both the para- and


FIG. 10. State-to-state cross sections for the vibrational quenching of CN from $\left(v_{1}=1, j_{1}=0\right)$ to $\left(v_{1}^{\prime}=0, j_{1}^{\prime}\right), j_{1}^{\prime}=0,2,4, \ldots, 24$, due to para $-\mathrm{H}_{2}$ $\left(v_{2}=0, j_{2}=0\right)$ collisions, or in CMS notation (1000) $\rightarrow\left(0 j_{1}^{\prime} 00\right), j_{2}=j^{\prime}{ }_{2}=0$.


FIG. 11. State-to-state cross sections for the vibrational quenching of CN from $\left(v_{1}=1, j_{1}=0\right)$ to $\left(v_{1}^{\prime}=0, j_{1}^{\prime}\right), j_{1}^{\prime}=0,2,4, \ldots, 24$, by ortho $-\mathrm{H}_{2}\left(v_{2}=0\right.$, $j_{2}=1$ ), or in CMS notation $(1001) \rightarrow\left(0 j_{1}^{\prime} 01\right), j_{2}=j^{\prime}{ }_{2}=1$.
ortho $-\mathrm{H}_{2}$ cases, the total vibrational quenching cross sections for elastic $\mathrm{H}_{2}$ processes are nearly an order of magnitude larger than that for collisions involving inelastic $\mathrm{H}_{2}$ transitions.

Total rate coefficients for the vibrational quenching of CN from (1000) to $\mathrm{CN}\left(v_{1}^{\prime}=0\right)+$ para $-\mathrm{H}_{2}\left(j_{2}^{\prime}=0\right.$ and 2$)$ and from (1001) to $\mathrm{CN}\left(v_{1}^{\prime}=0\right)+$ ortho $-\mathrm{H}_{2}\left(j_{2}^{\prime}=1\right.$ and 3$)$ are displayed in Fig. 13 for temperatures ranging from 5 to 300 K . The trends are similar to that given for the cross sections in Fig. 12. The total vibrational quenching rate coefficients of CN for $\Delta j_{2}=0$ are nearly an order of magnitude larger than the results for $\Delta j_{2}=2$. For the quenching due to para $-\mathrm{H}_{2}$ collisions, as shown in Fig. 13(a), between 5 and $\sim 100$ K, the rate coefficients generally decrease weakly with increasing temperature, while weak oscillatory temperature dependences are exhibited due to the presence of resonances. For temperatures above


FIG. 12. Total cross sections for the vibrational quenching of CN (a) from (1000) to $\mathrm{CN}\left(v_{1}^{\prime}=0\right)+$ para $-\mathrm{H}_{2}\left(j_{2}^{\prime}=0\right.$ and 2$)$. (b) From (1001) to CN $\left(v_{1}^{\prime}=0\right)+$ ortho $-\mathrm{H}_{2}\left(j_{2}^{\prime}=1\right.$ and 3$)$.


FIG. 13. Total rate coefficients for the vibrational quenching of CN compared to the same transitions for CO from Ref. 35. (a) From (1000) to $v_{1}^{\prime}=0$ + para $-\mathrm{H}_{2}\left(v_{2}=0, j_{2}^{\prime}=0,2\right)$. (b) From (1001) to $v_{1}^{\prime}=0+$ ortho $-\mathrm{H}_{2} \quad\left(v_{2}=0\right.$, $\left.j_{2}^{\prime}=1,3\right)$.
$\sim 100 \mathrm{~K}$, the rate coefficients increase with increasing temperature. The trends for ortho $-\mathrm{H}_{2}$ are very similar to those noted for para $-\mathrm{H}_{2}$ collisions. $\mathrm{CO}-\mathrm{H}_{2}$ rate coefficients ${ }^{35}$ for the same transitions are typically factors of $\sim 5-10$ smaller, as shown in Fig. 13. The smaller $\mathrm{CO}-\mathrm{H}_{2}$ rate coefficients are likely related to the fact that the $\mathrm{CN}-\mathrm{H}_{2}$ potential is more anisotropic, e.g., with global and local minima deeper by 38.69 and $11.12 \mathrm{~cm}^{-1}$, respectively.

## V. DISCUSSION

As highlighted in the Introduction, in astrophysical environments with intense UV fields, the radiation can drive the chemistry and internal level populations out of equilibrium. In such situations, a photodissociation region (PDR) resides at the interface of the hot $\mathrm{H}_{\text {II }}$ region and the cold molecular region. Sternberg and Dalgarno ${ }^{40}$ investigated the production of gas-phase atomic and molecular species in dense molecular clouds and identified molecular diagnostics of photondominated chemistry. It was illustrated that CN was formed by photodissociation of $\mathrm{HCN}, \mathrm{HCN}+v \rightarrow \mathrm{CN}+\mathrm{H}$, and by the reactions $\mathrm{NO}+\mathrm{C} \rightarrow \mathrm{CN}+\mathrm{O}$ and $\mathrm{C}+\mathrm{N} \rightarrow \mathrm{CN}+v$. Minor production of CN can also be obtained from dissociative recombination $\mathrm{H}_{2} \mathrm{CN}^{+}+e \rightarrow \mathrm{CN}+\mathrm{H}_{2}$. The CN abundance strongly depends on the UV radiation and increases in PDRs as the HCN photodissociation rate increases. Hence, CN emission lines may serve as useful diagnostics of PDRs.

Rodriguez-Franco and Martin-Pintado ${ }^{9}$ reported the observations of the CN 1-0 and 2-1 rotational emission towards the Orion A molecular complex and showed that the ionized gas of the H II region dominated the morphology of the CN emission. Aalto et al. ${ }^{10}$ detected CN 1-0 and 2-1 line emission in IR luminous galaxies and found that CN emission required
high density, $n>10^{4} \mathrm{~cm}^{-3}$. Therefore CN is expected to be a good tracer of high density regions and cold dense molecular clouds. This was also confirmed by Hakobian and Crutcher ${ }^{41}$ in their multi-species study of structure and composition of molecular clouds through the CN Zeeman transitions. Finally, Podio et al. ${ }^{42}$ argue that high $j_{1}$ lines, particularly the $5-4$, are unique tracers of embedded disks of young stellar objects, such as T Tau N .

We are, however, unaware of any CN vibrational transition observations though it is predicted to be abundant in models of protoplanetary disks ${ }^{43}$ and in the outflows of giant C- and O-rich evolved stars. ${ }^{44,45}$ It is anticipated that vibrational emission lines can probe the hot inner wind regions of the outflows and therefore provide information on the stellar mass-loss rates. ${ }^{44}$ With the upcoming launch of NASA's James Webb Space Telescope, the CN vibrational bands will become observable allowing astronomers to see deep into warm regions of these objects, particularly where the vibrational lines can be pumped by intense ultraviolet radiation. The collisional data computed here will be critical for models of such near infrared observations.

## VI. CONCLUSION

Accurate collisional rate coefficients for CN due to $\mathrm{H}_{2}$, needed for astrophysical modeling, are currently lacking for vibrationally excited CN . Quantum scattering calculations are the primary source of such rate coefficients, but accurate values that explicitly consider all six internal degrees of freedom of the $\mathrm{CN}-\mathrm{H}_{2}$ complex have not been reported due to the difficulty of the computations. We performed the first fulldimensional quantum dynamics calculations for inelastic rovibrational transitions of CN in collisions with $\mathrm{H}_{2}$ using a highlevel 6D PES. The PES was fitted with an invariant polynomial approach with an RMS error of less than $3.8 \mathrm{~cm}^{-1}$. Cross sections and rate coefficients for rotational (de)excitation of CN due to $\mathrm{H}_{2}$ and $\mathrm{D}_{2}$ collisions were studied using the new 6D PES for excited initial rotational levels of $\mathrm{CN}\left(j_{1}=4\right.$ and 11). Good agreement with the results of previous theoretical and experimental studies confirms the accuracy of the current PES fit and scattering calculations. We have carried out the first calculations of rovibrational quenching of CN $\left(v_{1}=1, j_{1}=0\right)$ in collisions with $\mathrm{H}_{2}\left(v_{2}=0, j_{2}=0,1,2\right)$ on the new 6D PES. To aid in astrophysical modeling, computations are in progress for a more highly excited vibrational level of $v_{1}=2$ of CN .

## SUPPLEMENTARY MATERIAL

See supplementary material ${ }^{46}$ for a Fortran subroutine to generate V6ES PES.

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${ }^{46}$ potV6ES.f is a Fortran subroutine to generate V6ES PES. Distances are in bohr, angles are in radian, and potential energy is in hartree. FitCoef.dat is the file for fitted coefficients of V6ES.

